

16.25. Model: Treat the helium gas in the sealed cylinder as an ideal gas.

Solve: The volume of the cylinder is $V = \pi r^2 h = \pi(0.05 \text{ m})^2(0.30 \text{ m}) = 2.356 \times 10^{-3} \text{ m}^3$. The gauge pressure of the gas is $120 \text{ psi} \times \frac{1 \text{ atm}}{14.7 \text{ psi}} \times \frac{1.013 \times 10^5 \text{ Pa}}{1 \text{ atm}} = 8.269 \times 10^5 \text{ Pa}$, so the absolute pressure of the gas is $8.269 \times 10^5 \text{ Pa} + 1.013 \times 10^5 \text{ Pa} = 9.282 \times 10^5 \text{ Pa}$. The temperature of the gas is $T = (273 + 20) \text{ K} = 293 \text{ K}$. The number of moles of the gas in the cylinder is

$$n = \frac{pV}{RT} = \frac{(9.282 \times 10^5 \text{ Pa})(2.356 \times 10^{-3} \text{ m}^3)}{(8.31 \text{ J/mol K})(293 \text{ K})} = 0.898 \text{ mol}$$

(a) The number of atoms is

$$N = nN_A = (0.898 \text{ mol})(6.02 \times 10^{23} \text{ mol}^{-1}) = 5.41 \times 10^{23} \text{ atoms.}$$

(b) The mass of the helium is

$$M = nM_{\text{mol}} = (0.898 \text{ mol})(4 \text{ g/mol}) = 3.59 \text{ g} = 3.59 \times 10^{-3} \text{ kg}$$

(c) The number density is

$$\frac{N}{V} = \frac{5.41 \times 10^{23} \text{ atoms}}{2.356 \times 10^{-3} \text{ m}^3} = 2.30 \times 10^{26} \text{ atoms/m}^3$$

(d) The mass density is

$$\rho = \frac{M}{V} = \frac{3.59 \times 10^{-3} \text{ kg}}{2.356 \times 10^{-3} \text{ m}^3} = 1.52 \text{ kg/m}^3$$